

# Contracting for Control

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- Post-GHM theory of the firm
  - Ownership for control (not bargaining or specific investments)
- Application to contract economics
  - Moving control rights across firm boundaries
- Testable implications?!
  - Benefit of adaptation → allocation of control
- Rich, tractable theoretical framework
  - Alliances, JVs, and other hybrid governance structures

## Analyses of Contract Terms (in Incomplete Contracts)

- Crocker, Goldberg, Klein, Masten, ...
- Lerner-Merges *JIE* 98
- Klein *REI* 00
- Arrunada-Garicano-Vázquez *JLEO* 01
- Kaplan-Stromberg *RES* 03
- Elfenbein-Lerner *RAND* 03
- Lerner-Shane-Tsai *JFE* 03

### Klein *REI* 00

- “Extend the simple model of self-enforcement to take account of the role of contract terms in facilitating self-enforcement.”
- “Court-enforcement and self-enforcement are complements in supply: the two mechanisms work better together than either of them does separately.”

# **Technical Appendix**

## **Decision Rights, Payoff Rights, and Relationships in Firms, Contracts, and Other Governance Structures**

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### **I. Spot Control**

- A. Elemental Model
- B. Alienable & Inalienable Decision Rights
- C. Assets (and Payoff Rights)
- D. Simple Governance Structures
- E. General Model
- F. Applications

## IA. Elemental Model

- Simon '51:
  - $d_0$  vs.  $d_B(s) \rightarrow d$  contractible  $\rightarrow$  renegotiation
- Updated approach:
  - *Decision right* contractible ex ante
  - *Decision* not contractible ex post
    - $\neq$  GHM
    - motivated by practitioners (BGM 03b “Alliances”)
    - other static models: BT 01, ADR 03, HH 03

- 2 parties  $i \in \{A, B\}$
- state  $s \in S$
- alienable dec. right  $d \in D$
- inalienable payoffs  $\pi_A(d, s), \pi_B(d, s)$
- $d^{FB}(s)$  solves  $\max_{d \in D} \pi_A(d, s) + \pi_B(d, s)$
- $V^{FB}(s) \equiv \pi_A(d^{FB}(s), s) + \pi_B(d^{FB}(s), s)$

- Control by  $i \in \{A, B\}$ :
  - $d_i^*(s)$  solves  $\max_{d \in D} \pi_i(d, s)$
  - $V_i(s) \equiv \pi_A(d_i^*(s), s) + \pi_B(d_i^*(s), s) \leq V^{FB}(s)$
- Efficient contract design:
  - $E[V_A(s)]$  vs  $E[V_B(s)]$

## IB. Alienable & Inalienable Decision Rights

- alienable DRs                       $\mathbf{d} = (d_1, \dots, d_J) \in \mathbf{D}$
- inalienable DRs                     $\delta_i \in \Delta_i, \boldsymbol{\delta} = (\delta_A, \delta_B)$
- inalienable payoffs                 $\pi_i(\mathbf{d}, \boldsymbol{\delta}, s)$
- Nash equilibrium                     $\mathbf{d}^{NE}(s), \boldsymbol{\delta}^{NE}(s)$

## IC. Assets (& Payoff Rights)

- *Asset*  $(D, \pi)$  (where  $\pi$  not contractible)
  - $d_i^*(s)$  solves  $\max_{d \in D} \pi_i(d, s) + \pi(d, s)$
  - $V_i(s) \equiv \pi_A(d_i^*(s), s) + \pi_B(d_i^*(s), s) + \pi(d_i^*(s), s)$
- *D separable* from  $\pi$ ?
  - pure PR vs. hidden DR?

## ID. Simple Governance Structures

- 2 alienable decision rights  $D_1, D_2$
- 2 alienable payoff rights  $\pi_1, \pi_2$
- 4 governance structures:
 

– A: $D_1, \pi_1$	B: $D_2, \pi_2$	non-integration?
– A: $D_1, \pi_1, D_2, \pi_2$	B: ---	integration?
– A: $D_1, \pi_1, D_2$	B: $\pi_2$	licensing?
– A: $D_1, \pi_1, \pi_2$	B: $D_2$	equity?
- *cf.* GHM:  $U_i(a_1, a_2, s, d_1, d_2)$

## IE. General Model

- I parties  $i \in I$   $\Delta_i, \pi_i$
- state  $s \in S$   $\sim f(s)$
- J assets  $j \in J$   $D_j, \pi_j$
- K decision rights  $k \in K$   $D_k$
- M payoff rights  $m \in M$   $\pi_m$
- *Governance structure*  $g \equiv$  allocation of assets, DRs, and PRs to parties  $\rightarrow \mathbf{D}_{ig}, \pi_{ig}$

## IF. Applications

- Ownership
- Contracts
- “Hybrids”

## II. Relational Control

- A. Relational Contracts
- B. Timing
- C. Equilibrium
- D. Constraint Reduction

### IIA. Relational Contracts

- Evidence: within & between firms
  - Macaulay '63, Macneil '78, Dore '83, Powell '90, ...
  - Barnard '38, Simon '47, Selznick '49, Gouldner '54 ...
- Theory, I: relational incentive contracts
  - Klein-Leffler '81, Telser '81, Bull '87
  - MacLeod-Malcomson '89, Levin '03
- Theory, II: formal and informal co-exist *and interact*
  - BGM '94, '99, '01, '02
  - Garvey '95, Halonen '02, Bragelien '03, Rayo '03



## IIB. Timing

1. Ex ante payment:  $t_{ig}$
2. State:  $s$
3. Post-state payment:  $\tau_{ig}(s)$
4. Decision:  $\mathbf{d}_{ig} \rightarrow \mathbf{d}^{RC}(\cdot) \rightarrow V^{RC}$
5. Post-decision payment:  $T_{ig}(d, s)$

## IIC. Equilibrium

- Trigger strategies
  - side-payment  $p_{ig} \rightarrow$  efficient spot governance after renegeing
- *Many* renegeing constraints:
  - example: will i pay  $t_{ig}$ ?

$$\begin{aligned}
 & [1+(1/r)] [t_{ig} + E_s \{ \pi_{ig}(\mathbf{d}^{RC}(s), s) + \tau_{ig}(s) + T_{ig}(\mathbf{d}^{RC}(s), s) \}] \\
 & \geq 0 + E_s \{ \pi_{ig}(\mathbf{d}^{NE}_g(s), s) + p_{ig}/(1+r) + (1/r)V_i^{SP} \}
 \end{aligned}$$

## IID. Constraint Reduction

(building on MM 89 & Levin 03)

$$\mathbf{d}_{ig}^{\text{DEV}}(s) = (\mathbf{d}_{ig}^{\text{BR}}(s), \mathbf{d}_{-ig}^{\text{RC}}(s))$$

$$R_{ig}(s) \equiv \pi_{ig}(\mathbf{d}_{ig}^{\text{DEV}}(s), s) - \pi_{ig}(\mathbf{d}^{\text{RC}}(s), s)$$

PROPOSITION:  $\mathbf{d}^{\text{RC}}(\cdot)$  feasible under  $g$  iff

$$\max_{s \in S} \sum_{i \in I} R_{ig}(s) < (1/r)[V^{\text{RC}} - V^{\text{SP}}]$$

## PAPER: Contracting for Control

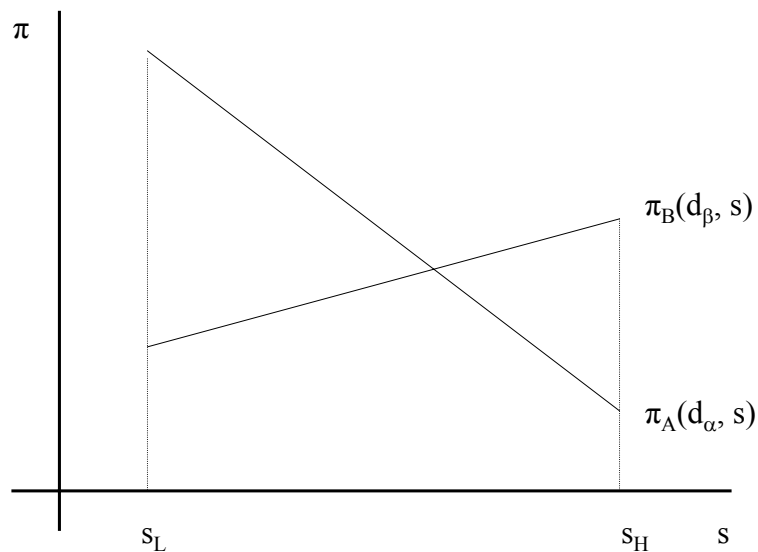
- I. Environment
- II. Spot Control
- III. First-best Relational Control
- IV. Second-best Relational Control
- V. Efficient Contract Design

# I. Environment

- 2 parties  $i \in \{A, B\}$
- state  $s \sim U[s_L, s_H]$
- alienable DR  $d \in \{d_\alpha, d_\beta\}$
- inalienable payoffs

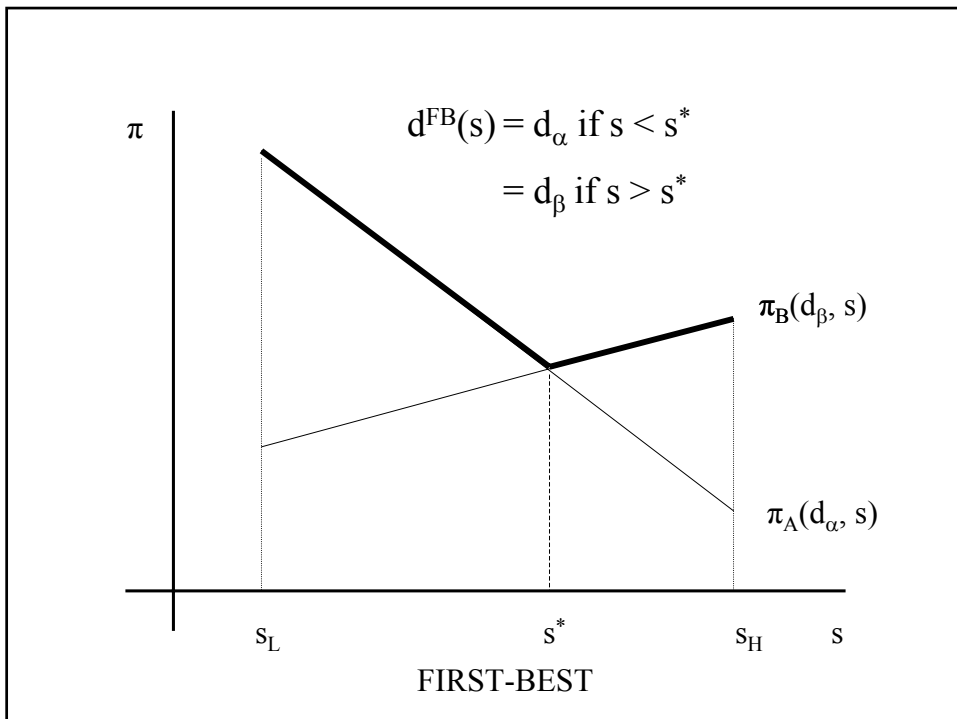
$$\pi_i(d_\iota, s) = \sigma_i s + \rho_i \quad i \in \{A, B\}$$

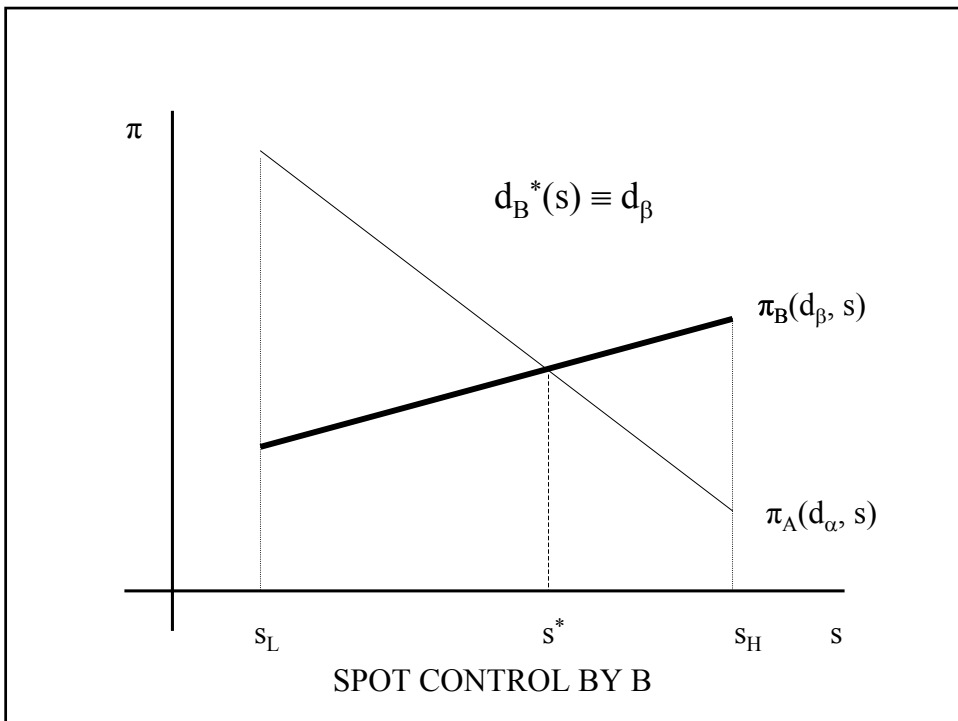
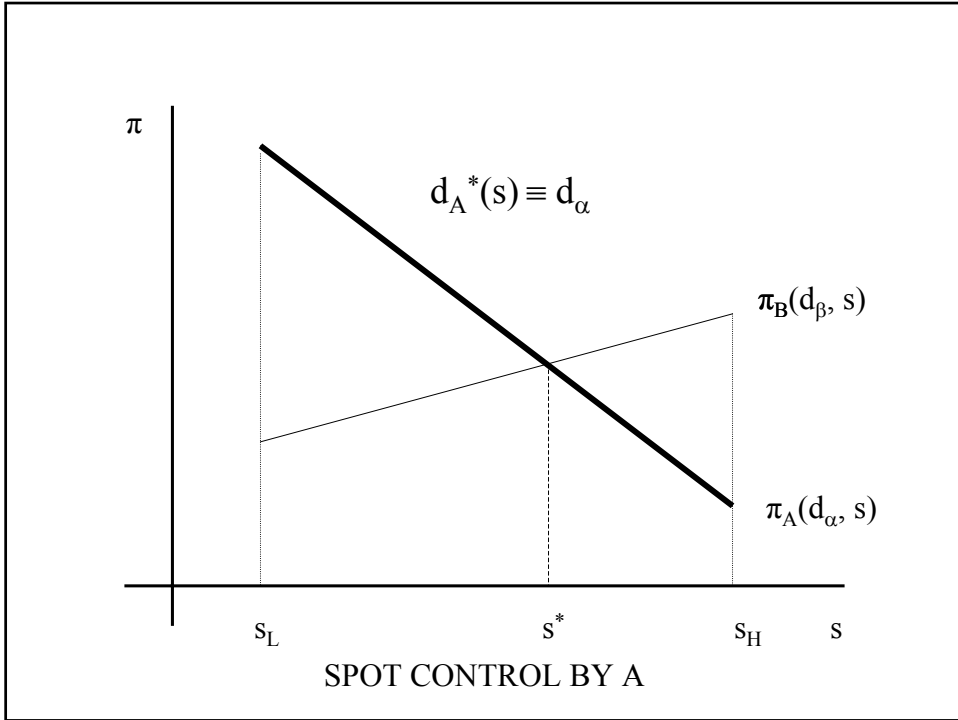
$$\pi_i(d_{-\iota}, s) = 0 \quad \iota \in \{\alpha, \beta\}$$

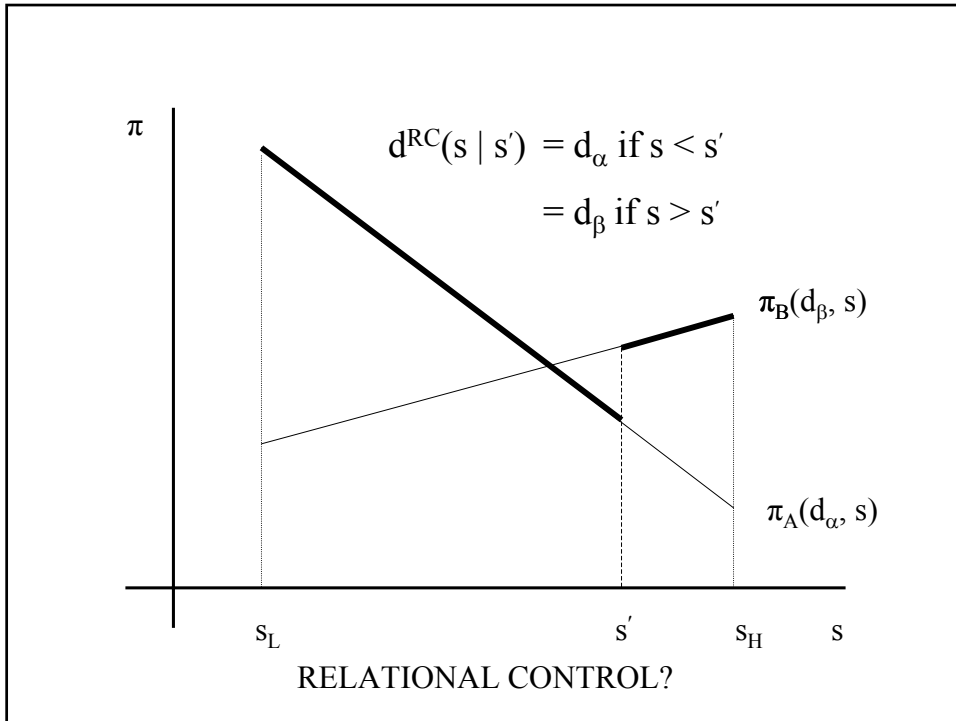


EXAMPLE

- generalizations:
  - $s \sim f(s)$
  - $\pi_i$  monotone
  - $\Pi_i = \pi_i(d, s) + k_i(s)$
- example parameters:
  - $\sigma_A < 0, \sigma_B > 0$
  - $SP \neq FB$







## II. Spot Control

- $i$  has control:

$$d_i^*(s) = d_i \text{ for all } s$$

$$V_i = \sigma_i E(s) + \rho_i$$

- efficient (spot) contract design:

$$V^{SP} \equiv \max \{ V_A, V_B \}$$

$$\rho_i = \text{benefit of unconditional control}$$

### III. FB Relational Control

- i has control:

$$R_i(s) = \pi_i(d_v, s) - \pi_i(d^{FB}(s), s)$$

$$\max_s R_i(s) = \pi_i(d_v, s^*) \equiv R^{FB}$$

- COROLLARY: FB feasible iff

$$R^{FB} < (1/r)[V^{FB} - V^{SP}]$$

### IV. SB Relational Control

- A has control:

$$d^{RC}(s | s') = d_\alpha \text{ if } s < s'$$

$$= d_\beta \text{ if } s > s'$$

$$\rightarrow V(s'), \quad R_A(s') = \pi_A(d_\alpha, s')$$

- COROLLARY:  $d^{RC}(\cdot | s')$  feasible by A iff

$$R_A(s') < (1/r)[V(s') - V^{SP}]$$

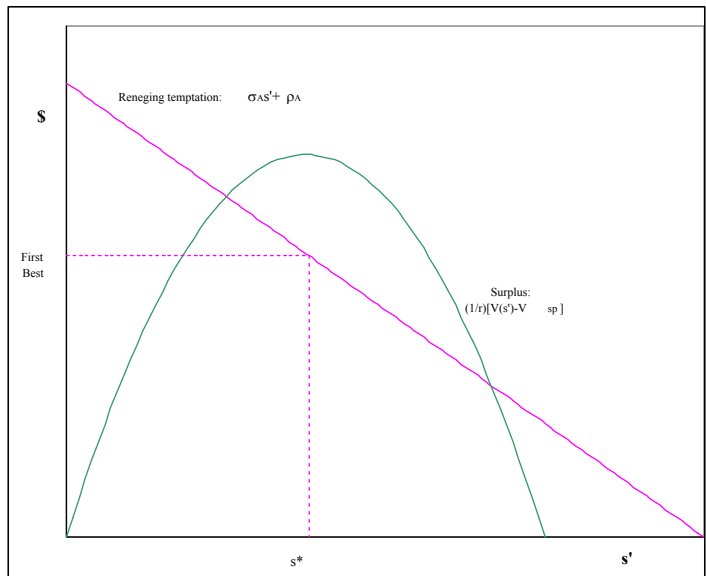
## SB Relational Control (cont.)

- If A has control:
  - Is  $d^{RC}(\cdot | s')$  optimal?
  - If so, what is the optimal  $s'$ ?
  - Iterated construction of  $SB_A$
- Should B have control?
  - (SB, SP) or (SP, SB) or (SB, SB)?

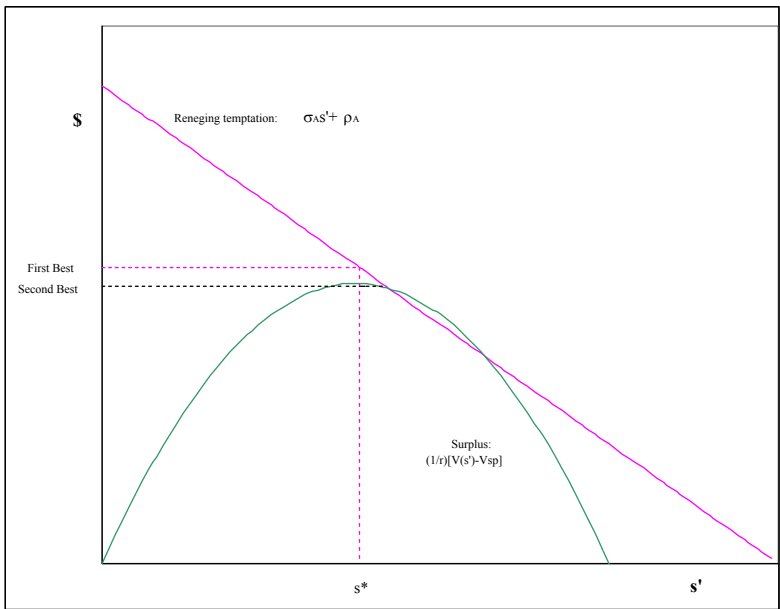
## V. Efficient Contract Design

- PROPOSITION:
  - Second-best relational control goes to  $\max \{|\sigma_A|, |\sigma_B|\}$
- Comparative statics
  - Macaulay, Coase '60, Klein I, Klein II

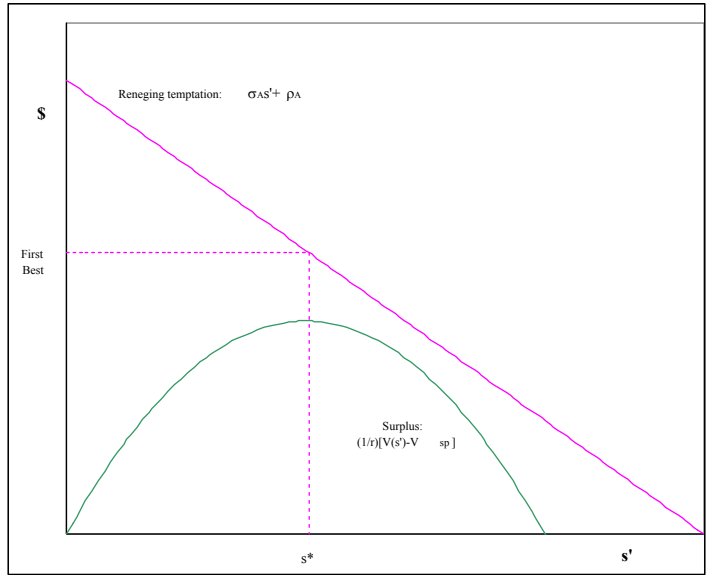




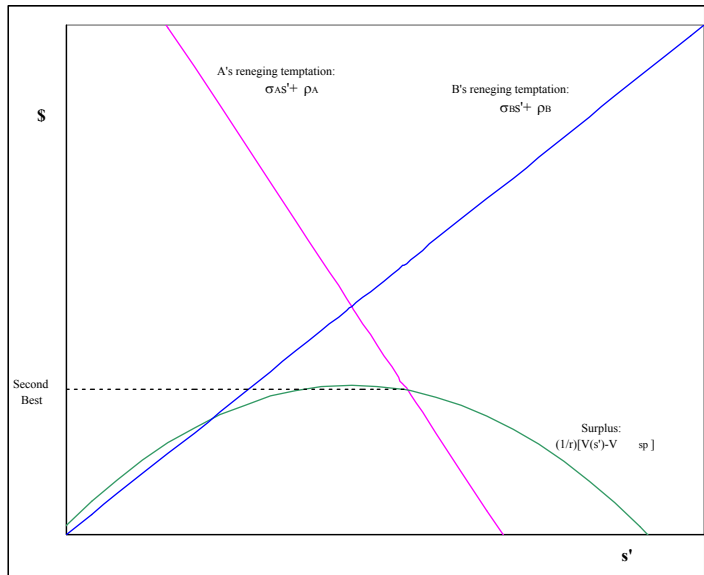
FIRST-BEST RELATIONAL CONTROL



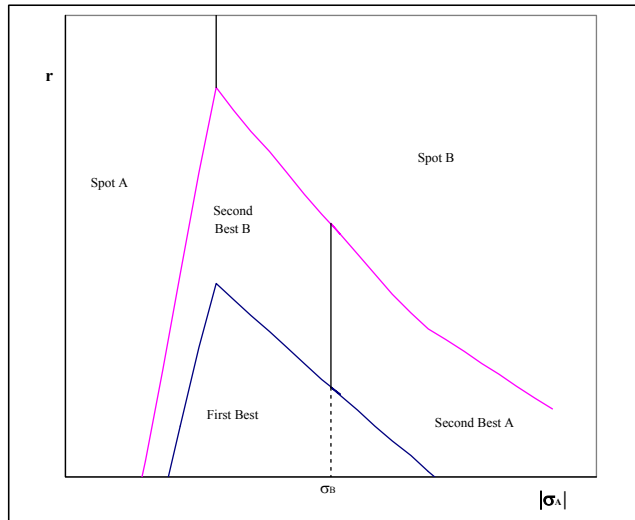
SECOND-BEST RELATIONAL CONTROL



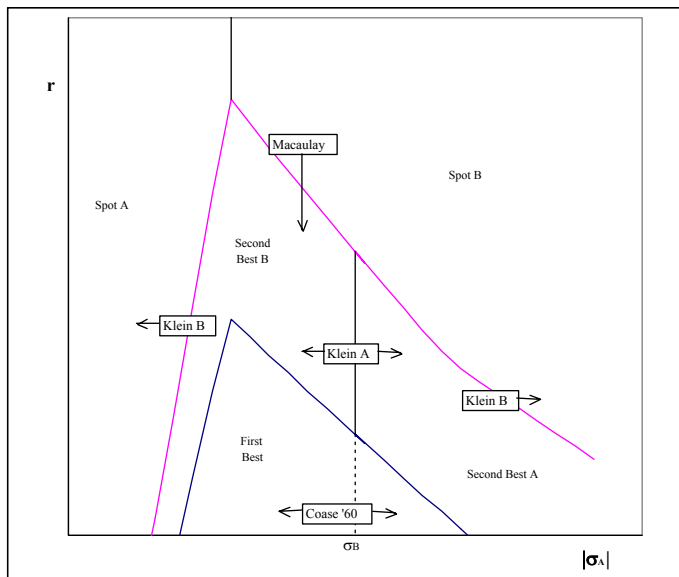
SPOT CONTROL BY A



SB BY A vs. SB BY B



EFFICIENT CONTRACT DESIGN



COMPARATIVE STATICS